Instruction Manual and Experiment Guide for the PASCO scientific Model TD-8553/8554A/8555

THERMAL RADIATION SYSTEM

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TD-854A Radiation Cube (Leslie's Cube)

TD-8555 Stefan Boltzman Lamp

TD-8553 Radiation Sensor

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$5.00
The lightning flash with arrowhead, within an equilateral triangle, is intended to alert the user of the presence of uninsulated “dangerous voltage” within the product’s enclosure that may be of sufficient magnitude to constitute a risk of electric shock to persons.

CAUTION:
TO PREVENT THE RISK OF ELECTRIC SHOCK, DO NOT REMOVE BACK COVER. NO USER SERVICEABLE PARTS INSIDE. REFER SERVICING TO QUALIFIED SERVICE PERSONNEL.

The exclamation point within an equilateral triangle is intended to alert the user of the presence of important operating and maintenance (servicing) instructions in the literature accompanying the appliance.
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2. Make certain there are at least two inches of packing material between any point on the apparatus and the inside walls of the carton.
3. Make certain that the packing material cannot shift in the box or become compressed, allowing the instrument come in contact with the packing carton.

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Introduction

The PASCO Thermal Radiation System includes three items: the TD-8553 Radiation Sensor, the TD-8554A Radiation Cube (Leslie's Cube), and the TD-8555 Stefan-Boltzmann Lamp. This manual contains operating instructions for each of these items plus instructions and worksheets for the following four experiments:

1. Introduction to Thermal Radiation,
2. Inverse Square Law,
3. Stefan-Boltzmann Law* (at high temperatures),

* The Stefan-Boltzmann law states that the radiant energy per unit area is proportional to the fourth power of the temperature of the radiating surface.

In addition to the equipment in the radiation system, several standard laboratory items, such as power supplies and meters are needed for most experiments. Check the experiment section of this manual for information on required equipment.

If you don't have all the items of the radiation system, read through the operating instructions for the equipment you do have, then check the experiment section to determine which of the experiments you can perform. (A radiation sensor is required for all the experiments.)

Radiation Sensor

The PASCO TD-8553 Radiation Sensor (Figure 1) measures the relative intensities of incident thermal radiation. The sensing element, a miniature thermopile, produces a voltage proportional to the intensity of the radiation. The spectral response of the thermopile is essentially flat in the infrared region (from 0.5 to 40 μm), and the voltages produced range from the microvolt range up to around 100 millivolts. (A good millivolt meter is sufficient for all the experiments described in this manual. See the current PASCO catalog for recommended meters.)

The Sensor can be hand held or mounted on its stand for more accurate positioning. A spring-clip shutter is opened and closed by sliding the shutter ring forward or back. During experiments, the shutter should be closed when measurements are not actively being taken. This helps reduce temperature shifts in the thermopile reference junction which can cause the sensor response to drift.

**NOTE:** When opening and closing the shutter, it is possible you may inadvertently change the sensor position. Therefore, for experiments in which the sensor position is critical, such as Experiment 3, two small sheets of opaque insulating foam have been provided. Place this heat shield in front of the sensor when measurements are not actively being taken.

The two posts extending from the front end of the Sensor protect the thermopile and also provide a reference for positioning the sensor a repeatable distance from a radiation source.

Specifications

- Temperature Range: -65 to 85 °C.
- Maximum Incident Power: 0.1 Watts/cm².
- Spectral Response: .6 to 30μm.
- Signal Output: Linear from $10^{-6}$ to $10^{-1}$ Watts/cm².

![Figure 1 Radiation Sensor](image-url)
The TD-8554A Radiation Cube (Figure 2) provides four different radiating surfaces that can be heated from room temperature to approximately 120 °C. The cube is heated by a 100 watt light bulb. Just plug in the power cord, flip the toggle switch to “ON”, then turn the knob clockwise to vary the power.

Measure the cube temperature by plugging your ohmmeter into the banana plug connectors labeled THERMISTOR. The thermistor is embedded in one corner of the cube. Measure the resistance, then use Table 1, below, to translate the resistance reading into a temperature measurement. An abbreviated version of this table is printed on the base of the Radiation Cube.

**NOTE:** For best results, a digital ohmmeter should be used. (See the current PASCO catalog for recommended meters.)

**IMPORTANT:** When replacing the light bulb, use a 100-Watt bulb. Bulbs of higher power could damage the cube.

![Figure 2 Radiation Cube (Leslie's Cube)](image)

### Table 1: Resistance versus Temperature for the Thermal Radiation Cube

<table>
<thead>
<tr>
<th></th>
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<th></th>
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<td>10</td>
<td>197,560</td>
<td>11</td>
<td>187,840</td>
<td>12</td>
<td>178,650</td>
<td>13</td>
<td>169,950</td>
<td>14</td>
</tr>
<tr>
<td>153,950</td>
<td>15</td>
<td>146,580</td>
<td>17</td>
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<td>87,022</td>
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<td>79,422</td>
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<td>75,903</td>
<td>31</td>
<td>72,560</td>
<td>32</td>
<td>69,380</td>
<td>33</td>
</tr>
</tbody>
</table>

![Table 1](image)
Stefan-Boltzmann Lamp

**IMPORTANT:** The voltage into the lamp should **NEVER exceed 13 V**. Higher voltages will burn out the filament.

The TD-8555 Stefan-Boltzmann Lamp (Figure 3) is a high temperature source of thermal radiation. The lamp can be used for high temperature investigations of the Stefan-Boltzmann Law. The high temperature simplifies the analysis because the fourth power of the ambient temperature is negligibly small compared to the fourth power of the high temperature of the lamp filament (see Experiments 3 and 4). When properly oriented, the filament also provides a good approximation to a point source of thermal radiation. It therefore works well for investigations into the inverse square law.

By adjusting the power into the lamp (13 Volts max, 2 A min, 3 A max), filament temperatures up to approximately 3,000 °C can be obtained. The filament temperature is determined by carefully measuring the voltage and current into the lamp. The voltage divided by the current gives the resistance of the filament.

**Equipment Recommended**

AC/DC LV Power Supply (SF-9584) or equivalent capable of 13 V @ 3 A max

\[ T = \frac{R - R_{\text{ref}}}{\alpha R_{\text{ref}}} + T_{\text{ref}} \]

For small temperature changes, the temperature of the tungsten filament can be calculated using \( \alpha \), the temperature coefficient of resistivity for the filament:

- \( T = \) Temperature
- \( R = \) Resistance at temperature \( T \)
- \( T_{\text{ref}} = \) Reference temperature (usually room temp.)
- \( R_{\text{ref}} = \) Resistance at temperature \( T_{\text{ref}} \)
- \( \alpha = \) Temperature coefficient of resistivity for the filament (\( \alpha = 4.5 \times 10^{-3} \, \text{K}^{-1} \) for tungsten)

For large temperature differences, however, \( \alpha \) is not constant and the above equation is not accurate.

**For large temperature differences**, therefore, determine the temperature of the tungsten filament as follows:

1. Accurately measure the resistance \( (R_{\text{ref}}) \) of the tungsten filament at room temperature (about 300 °K). Accuracy is important here. A small error in \( R_{\text{ref}} \) will result in a large error in your result for the filament temperature.

2. When the filament is hot, measure the voltage and current into the filament and divide the voltage by the current to measure the resistance \( (R_T) \).

3. Divide \( R_T \) by \( R_{\text{ref}} \) to obtain the relative resistance \( (R_T/R_{\text{ref}}) \).

4. Using your measured value for the relative resistivity of the filament at temperature \( T \), use Table 2 on the following page, or the associated graph, to determine the temperature of the filament.

** REPLACEMENT BULB:** GE Lamp No. 1196, available at most auto parts stores.

** NOTE:** When replacing the bulb, the leads should be soldered to minimize resistance.
### Table 2: Temperature and Resistivity for Tungsten

<table>
<thead>
<tr>
<th>$R/R_{300K}$</th>
<th>Temp °K</th>
<th>Resistivity $\mu\Omega$ cm</th>
<th>$R/R_{300K}$</th>
<th>Temp °K</th>
<th>Resistivity $\mu\Omega$ cm</th>
<th>$R/R_{300K}$</th>
<th>Temp °K</th>
<th>Resistivity $\mu\Omega$ cm</th>
</tr>
</thead>
<tbody>
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<td>1.0</td>
<td>300</td>
<td>5.65</td>
<td>5.48</td>
<td>1200</td>
<td>30.98</td>
<td>10.63</td>
<td>2100</td>
<td>60.06</td>
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<tr>
<td>1.43</td>
<td>400</td>
<td>8.06</td>
<td>6.03</td>
<td>1300</td>
<td>34.08</td>
<td>11.24</td>
<td>2200</td>
<td>63.48</td>
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<tr>
<td>1.87</td>
<td>500</td>
<td>10.56</td>
<td>6.58</td>
<td>1400</td>
<td>37.19</td>
<td>11.84</td>
<td>2300</td>
<td>66.91</td>
</tr>
<tr>
<td>2.34</td>
<td>600</td>
<td>13.23</td>
<td>7.14</td>
<td>1500</td>
<td>40.36</td>
<td>12.46</td>
<td>2400</td>
<td>70.39</td>
</tr>
<tr>
<td>2.85</td>
<td>700</td>
<td>16.09</td>
<td>7.71</td>
<td>1600</td>
<td>43.55</td>
<td>13.08</td>
<td>2500</td>
<td>73.91</td>
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<td>3.36</td>
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<td>8.28</td>
<td>1700</td>
<td>46.78</td>
<td>13.72</td>
<td>2600</td>
<td>77.49</td>
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<td>3.88</td>
<td>900</td>
<td>21.94</td>
<td>8.86</td>
<td>1800</td>
<td>50.05</td>
<td>14.34</td>
<td>2700</td>
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<td>4.41</td>
<td>1000</td>
<td>24.93</td>
<td>9.44</td>
<td>1900</td>
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<td>2000</td>
<td>56.67</td>
<td>15.63</td>
<td>2900</td>
<td>88.33</td>
</tr>
</tbody>
</table>

#### Temperature versus Resistivity for Tungsten

![Graph of Temperature versus Resistivity for Tungsten](image_url)
Experiment 1: Introduction to Thermal Radiation

EQUIPMENT NEEDED:

— Radiation Sensor, Thermal Radiation Cube
— Millivoltmeter
— Window glass
— Ohmmeter.

NOTES:

1. If lab time is short, it’s helpful to preheat the cube at a setting of 5.0 for 20 minutes before the laboratory period begins. (A very quick method is to preheat the cube at full power for 45 minutes, then use a small fan to reduce the temperature quickly as you lower the power input. Just be sure that equilibrium is attained with the fan off.)

2. Part 1 and 2 of this experiment can be performed simultaneously. Make the measurements in Part 2 while waiting for the Radiation Cube to reach thermal equilibrium at each of the settings in Part 1.

3. When using the Radiation Sensor, always shield it from the hot object except for the few seconds it takes to actually make the measurement. This prevents heating of the thermopile which will change the reference temperature and alter the reading.

Radiation Rates from Different Surfaces

Part 1

1. Connect the Ohmmeter and Millivoltmeter as shown in Figure 1.1.

2. Turn on the Thermal Radiation Cube and set the power switch to “HIGH”. Keep an eye on the ohmmeter reading. When it gets down to about 40 kΩ, reset the power switch to 5.0. (If the cube is preheated, just set the switch to 5.0.)

3. When the cube reaches thermal equilibrium—the ohmmeter reading will fluctuate around a relatively fixed value—use the Radiation Sensor to measure the radiation emitted from each of the four surfaces of the cube. Place the Sensor so that the posts on its end are in contact with the cube surface (this ensures that the distance of the measurement is the same for all surfaces). Record your measurements in the appropriate table on the following page. Also measure and record the resistance of the thermistor. Use the table on the base of the cube to determine the corresponding temperature.

4. Increase the power switch setting, first to 6.5, then to 8.0, then to “HIGH”. At each setting, wait for the cube to reach thermal equilibrium, then repeat the measurements of step 1 and record your results in the appropriate table.
Part 2

Use the Radiation Sensor to examine the relative magnitudes of the radiation emitted from various objects around the room. On a separate sheet of paper, make a table summarizing your observations. Make measurements that will help you to answer the questions listed below.

Absorption and Transmission of Thermal Radiation

① Place the Sensor approximately 5 cm from the black surface of the Radiation Cube and record the reading. Place a piece of window glass between the Sensor and the bulb. Does window glass effectively block thermal radiation?

② Remove the lid from the Radiation Cube (or use the Stefan-Boltzmann Lamp) and repeat the measurements of step 1, but using the bare bulb instead of the black surface. Repeat with other materials.

Radiation Rates from Different Surfaces

Data and Calculations

<table>
<thead>
<tr>
<th>Power Setting</th>
<th>Therm. Res. Temperature</th>
<th>Surface</th>
<th>Sensor Reading (mV)</th>
<th>Therm. Res. Temperature</th>
<th>Surface</th>
<th>Sensor Reading (mV)</th>
<th>Therm. Res. Temperature</th>
<th>Surface</th>
<th>Sensor Reading (mV)</th>
<th>Therm. Res. Temperature</th>
<th>Surface</th>
<th>Sensor Reading (mV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>5.0</td>
<td>Ω</td>
<td>Black</td>
<td></td>
<td>Ω</td>
<td>White</td>
<td></td>
<td>Ω</td>
<td>Polished Aluminum</td>
<td></td>
<td>Ω</td>
<td>Dull Aluminum</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>White</td>
<td></td>
<td></td>
<td>White</td>
<td></td>
<td></td>
<td>Polished Aluminum</td>
<td></td>
<td></td>
<td>Dull Aluminum</td>
<td></td>
</tr>
</tbody>
</table>
Questions (Part 1)

① List the surfaces of the Radiation Cube in order of the amount of radiation emitted. Is the order independent of temperature?

② It is a general rule that good absorbers of radiation are also good emitters. Are your measurements consistent with this rule? Explain.

Questions (Part 2)

① Do different objects, at approximately the same temperature, emit different amounts of radiation?

② Can you find materials in your room that block thermal radiation? Can you find materials that don’t block thermal radiation? (For example, do your clothes effectively block the thermal radiation emitted from your body?)

Absorption and Transmission of Thermal Radiation

Questions

① What do your results suggest about the phenomenon of heat loss through windows?

② What do your results suggest about the Greenhouse Effect?
Experiment 2: Inverse Square Law

EQUIPMENT NEEDED:
— Radiation Sensor
— Stefan-Boltzmann Lamp, Millivoltmeter
— Power Supply (12 VDC; 3 A), meter stick.

1. Set up the equipment as shown in Figure 2.1.
   a. Tape a meter stick to the table.
   b. Place the Stefan-Boltzmann Lamp at one end of the meter stick as shown. The zero-point of the meter stick should align with the center of the lamp filament.
   c. Adjust the height of the Radiation Sensor so it is at the same level as the filament of the Stefan-Boltzmann Lamp.
   d. Align the lamp and sensor so that, as you slide the Sensor along the meter stick, the axis of the lamp aligns as closely as possible with the axis of the Sensor.
   e. Connect the Sensor to the millivoltmeter and the lamp to the power supply as indicated in the figure.

2. With the lamp OFF, slide the sensor along the meter stick. Record the reading of the millivolt-meter at 10 cm intervals. Record your values in Table 2.1 on the following page. Average these values to determine the ambient level of thermal radiation. You will need to subtract this average ambient value from your measurements with the lamp on, in order to determine the contribution from the lamp alone.

3. Turn on the power supply to illuminate the lamp. Set the voltage to approximately 10 V.
**IMPORTANT:** Do not let the voltage to the lamp exceed 13 V.

Adjust the distance between the Sensor and the lamp to each of the settings listed in Table 2.2. At each setting, record the reading on the millivoltmeter.

**IMPORTANT:** Make each reading quickly. Between readings, move the Sensor away from the lamp, or place the reflective heat shield between the lamp and the Sensor, so that the temperature of the Sensor stays relatively constant.

<table>
<thead>
<tr>
<th>X (cm)</th>
<th>Ambient Radiation Level (mV)</th>
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</thead>
<tbody>
<tr>
<td>10</td>
<td>2.5</td>
</tr>
<tr>
<td>20</td>
<td>3.0</td>
</tr>
<tr>
<td>30</td>
<td>3.5</td>
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<tr>
<td>40</td>
<td>4.0</td>
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<td>50</td>
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<tr>
<td>70</td>
<td>6.0</td>
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<tr>
<td>80</td>
<td>7.0</td>
</tr>
<tr>
<td>90</td>
<td>8.0</td>
</tr>
<tr>
<td>100</td>
<td>9.0</td>
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</tbody>
</table>

Average Ambient Radiation Level =

---

Table 2.1
Ambient Radiation Level

<table>
<thead>
<tr>
<th>X (cm)</th>
<th>Rad (mV)</th>
<th>1/X^2 (cm^-2)</th>
<th>Rad - Ambient (mV)</th>
</tr>
</thead>
<tbody>
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<td>2.5</td>
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<tr>
<td>100.0</td>
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<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2.2
Radiation Level versus Distance
Calculations

1. For each value of X, calculate \( \frac{1}{X^2} \). Enter your results in Table 2.2.

2. Subtract the Average Ambient Radiation Level from each of your Rad measurements in Table 2.2. Enter your results in the table.

3. On a separate sheet of paper, make a graph of Radiation Level versus Distance from Source, using columns one and four from Table 2.2. Let the radiation level be the dependent (y) axis.

4. If your graph from part 3 is not linear, make a graph of Radiation Level versus \( \frac{1}{X^2} \), using columns three and four from table 2.2.

Questions

1. Which of the two graphs is more linear? Is it linear over the entire range of measurements?

2. The inverse square law states that the radiant energy per unit area emitted by a point source of radiation decreases as the square of the distance from the source to the point of detection. Does your data support this assertion?

3. Is the Stefan-Boltzmann Lamp truly a point source of radiation? If not, how might this affect your results? Do you see such an effect in the data you have taken?
Experiment 3: Stefan-Boltzmann Law (high temperature)

EQUIPMENT NEEDED:
— Radiation Sensor
— Ohmmeter
— Stefan-Boltzmann Lamp
— Voltmeter (0-12 V)
— Ammeter (0-3 A)
— Millivoltmeter
— Ohmmeter
— Thermometer.

Introduction

The Stefan-Boltzmann Law relates R, the power per unit area radiated by an object, to T, the absolute temperature of the object. The equation is:

\[ R = \sigma T^4; \quad \left( \sigma = 5.6703 \times 10^{-8} \frac{W}{m^2 K^4} \right) \]

In this experiment, you will make relative measurements of the power per unit area emitted from a hot object, namely the Stefan-Boltzmann Lamp, at various temperatures. From your data you will be able to test whether the radiated power is really proportional to the fourth power of the temperature.

Most of the thermal energy emitted by the lamp comes from the filament of the lamp. The filament temperature can be determined using the procedure given on pages 3 and 4 of this manual.

Figure 3.1 Equipment Setup
Procedure

➤ **IMPORTANT:** The voltage into the lamp should NEVER exceed 13 V. Higher voltages will burn out the filament.

1. **BEFORE TURNING ON THE LAMP**, measure $T_{\text{ref}}$, the room temperature in degrees Kelvin, $(K=^\circ C + 273)$ and $R_{\text{ref}}$, the resistance of the filament of the Stefan-Boltzmann Lamp at room temperature. Enter your results in the spaces on the following page.

2. Set up the equipment as shown in Figure 3.1. The voltmeter should be connected directly to the binding posts of the Stefan-Boltzmann Lamp. The Sensor should be at the same height as the filament, with the front face of the Sensor approximately 6 cm away from the filament. The entrance angle of the thermopile should include no close objects other than the lamp.

3. Turn on the power supply. Set the voltage, $V$, to each of the settings listed in Table 3.1 on the following page. At each voltage setting, record $I$, the ammeter reading, and $R_{\text{d}}$, the reading on the millivoltmeter.

➤ **IMPORTANT:** Make each Sensor reading quickly. Between readings, place both sheets of insulating foam between the lamp and the Sensor, with the silvered surface facing the lamp, so that the temperature of the Sensor stays relatively constant.
Data and Calculations

1. Calculate R, the resistance of the filament at each of the voltage settings used (R = V/I).
   Enter your results in Table 3.1.

2. Use the procedure on pages 3 and 4 of this manual to determine T, the temperature of the lamp filament at each voltage setting. Enter your results in the table.

3* Calculate T^4 for each value of T and enter your results in the table.

4* On a separate sheet of paper, construct a graph of Rad versus T^4. Use Rad as your dependent variable (y-axis).

*In place of calculations 1 and 2, some may prefer to perform a power regression on Rad versus T to determine their relationship, or graph on log-log paper and find the slope.

Questions

1. What is the relationship between Rad and T? Does this relationship hold over the entire range of measurements?

2. The Stefan-Boltzmann Law is perfectly true only for ideal, black body radiation. A black body is any object that absorbs all the radiation that strikes it. Is the filament of the lamp a true black body?

3. What sources of thermal radiation, other than the lamp filament, might have influenced your measurements? What affect would you expect these sources to have on your results?

\[ \alpha = 4.5 \times 10^{-3} \text{ K}^{-1} \]

\[ T_{\text{ref}} \text{ (room temperature)} = \ldots \text{ K} \ (K = ^\circ C + 273) \]

\[ R_{\text{ref}} \text{ (filament resistance at } T_{\text{ref}}) = \ldots \Omega \]

<table>
<thead>
<tr>
<th>Data</th>
<th>Calculations</th>
</tr>
</thead>
<tbody>
<tr>
<td>V (Volts)</td>
<td>I (Amps)</td>
</tr>
<tr>
<td>1.00</td>
<td></td>
</tr>
<tr>
<td>2.00</td>
<td></td>
</tr>
<tr>
<td>3.00</td>
<td></td>
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<tr>
<td>4.00</td>
<td></td>
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<tr>
<td>5.00</td>
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<tr>
<td>6.00</td>
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<tr>
<td>7.00</td>
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<tr>
<td>8.00</td>
<td></td>
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<tr>
<td>9.00</td>
<td></td>
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<tr>
<td>10.00</td>
<td></td>
</tr>
<tr>
<td>11.00</td>
<td></td>
</tr>
<tr>
<td>12.00</td>
<td></td>
</tr>
</tbody>
</table>
Experiment 4: Stefan-Boltzmann Law (low temperature)

EQUIPMENT NEEDED:
— Radiation Sensor
— Millivoltmeter
— Thermal Radiation Cube
— Ohmmeter.

Introduction

In experiment 3, you investigated the Stefan-Boltzmann Law \( R_{rad} = sT^4 \) for the high temperatures attained by an incandescent filament. At those high temperatures (approximately 1,000 to 3,000 K), the ambient temperature is small enough that it can be neglected in the analysis. In this experiment you will investigate the Stefan-Boltzmann relationship at much lower temperatures using the Thermal Radiation Cube. At these lower temperatures, the ambient temperature can not be ignored.

If the detector in the Radiation Sensor were operating at absolute zero temperature, it would produce a voltage directly proportional to the intensity of the radiation that strikes it. However, the detector is not at absolute zero temperature so it is also radiating thermal energy. According to the Stefan-Boltzmann law, it radiates at a rate, \( R_{det} = sT_{det}^4 \). The voltage produced by the sensor is proportional to the radiation striking the detector minus the radiation leaving it. Mathematically, the sensor voltage is proportional to \( R_{net} = R_{rad} - R_{det} = s(T^4 - T_{det}^4) \). As long as you are careful to shield the Radiation Sensor from the Radiation Cube when measurements are not being taken, \( T_{det} \) will be very close to room temperature \( (T_{rm}) \).

Procedure

1. Set up the equipment as shown in Figure 4.1. The Radiation Sensor should be pointed directly at the center of one of the better radiating surfaces of the cube (the black or white surface). The face of the Sensor should be parallel with the surface of the cube and about 3 to 4 cm away.

2. With the Thermal Radiation Cube off, measure \( R_{rm} \), the resistance of the thermistor at room temperature. Enter this data in the space on the following page.

3. Shield the sensor from the cube using the reflecting heat shield, with the reflective side of the shield facing the cube.

4. Turn on the Radiation Cube and set the power switch to 10.

5. When the thermistor resistance indicates that the temperature is about 12 C° above room temperature, turn the power down so the temperature is changing slowly. Read and record \( R \), the ohmmeter reading, and \( Rad \), the millivoltmeter reading. The readings should be taken as nearly simultaneously as possible while briefly removing the heat shield. Record these values in Table 4.1.
**IMPORTANT:** Make each reading quickly, removing the heat shield only as long as it takes to make the measurement. Take care that the position of the sensor with respect to the cube is the same for all measurements.

Replace the heat shield, and turn the cube power to 10. When the temperature has risen an additional 12-15°C, repeat the measurements of step 5. Repeat this procedure at about 12-15°C intervals until the maximum temperature of the cube is reached.

### Data and Calculations

**Room Temperature:** \( R_{\text{rm}} = \ldots\ \Omega \)

\[ T_{\text{rm}} = \ldots \ ^\circ\text{C} = \ldots \ K \]

| Table 4.1 |
|---|---|---|---|---|---|
| Data | Calculations |
| R \((\text{y' \text{v}})\) | Rad \((\text{mV})\) | \( T_c \) \((^\circ\text{C})\) | \( T_k \) \((K)\) | \( T_k^4 \) \((K^4)\) | \( T_k^4 - T_{\text{rm}}^4 \) \((K^4)\) |

1. Using the table on the base of the Thermal Radiation Cube, determine \( T_c \), the temperature in degrees Centigrade corresponding to each of your thermistor resistance measurements. For each value of \( T_c \), determine \( T_k \), the corresponding value in degrees Kelvin \((K = ^{\circ}C + 273)\). Enter both sets of values in Table 4.1, above. In the same manner, determine the room temperature, \( T_{\text{rm}} \).
2. Calculate \( T_k^4 \) for each value of \( T_k \) and record the values in the table.
3. Calculate \( T_k^4 - T_{\text{rm}}^4 \) for each value of \( T_k \) and record your results in the table.
4. On separate sheet of paper, construct a graph of Rad versus \( T_k^4 - T_{\text{rm}}^4 \). Use Rad as the dependent variable \((y\text{-axis})\).

### Questions

1. What does your graph indicate about the Stefan-Boltzmann law at low temperatures?
2. Is your graph a straight line? Discuss any deviations that exist.
Teacher’s Guide

Experiment 1: Introduction to Thermal Radiation

Notes on Questions

Part 1

1. In order of decreasing emissivity, the surfaces are Black, White, Dull Aluminum, and Polished Aluminum. This order is independent of temperature; and within the temperature range tested, the ratio of emissions between sides is almost constant. The normalized percentages are as follows: (Black is defined as 100%)

<table>
<thead>
<tr>
<th>Surface</th>
<th>Normalized Emissions</th>
<th>Standard Error</th>
</tr>
</thead>
<tbody>
<tr>
<td>Black</td>
<td>100</td>
<td></td>
</tr>
<tr>
<td>White</td>
<td>96.86 ±1.21%</td>
<td></td>
</tr>
<tr>
<td>Dull</td>
<td>20.23 ±2.17%</td>
<td></td>
</tr>
<tr>
<td>Polished</td>
<td>7.38 ±1.82%</td>
<td></td>
</tr>
</tbody>
</table>

2. Measurements are consistent with the rule. The better reflectors (poorer absorbers) are poor emitters.

Notes on Questions

Part 2

1. Yes. All sides of the Leslie’s Cube are at the same temperature, but the polished side emits less than 10% as much radiation as the black side.

2. Materials that block thermal radiation well include aluminum foil, styrofoam, etc. Materials that do not block radiation as well include air, clothing, etc. All materials will block radiation to some degree, but there are strong differences in how much is blocked.

Notes on Questions

Absorption and Transmission of Thermal Radiation

1. Heat loss through (closed) windows is primarily conductive. Although the glass tested transmitted some infrared, most was blocked.

2. A greenhouse allows light in, but does not allow much heat to escape. This phenomenon is used to grow tropical plants in cold climates.

Experiment 2: Inverse Square Law

Calculations

$R^2 = 9.822989E-1$

$f(x) = 2.060229E+2 \cdot (x^{-1.815646E+0})$

A greenhouse allows light in, but does not allow much heat to escape. This phenomenon is used to grow tropical plants in cold climates.
Notes on Questions

1. The graph of Radiation versus 1/x^2 is more linear, but not over the entire range. There is a distinct falloff in intensity at the nearer distances, due to the non-point characteristics of the lamp. (A graph of Radiation versus 1/x^2 using only data points from 10cm or more is nearly linear.)

2. If we use data from distances that are large compared to the size of the lamp filament—so that the filament is effectively a “point”—then this data supports the hypothesis.

3. The Stefan-Boltzmann Lamp is not truly a point source. If it were not, then there would be a falloff in light level for measurements taken close to the lamp. This falloff can be seen in our data.

Suggestion:

The largest part of the error in this lab is due to the non-point nature of the Stefan-Boltzmann Lamp. You can approximate a much better “point” source with a laser and a converging lens.

For best results, use a short-focal-length lens and make sure that the sensor is always completely within the beam.

---

### Experiment 3: Stefan-Boltzmann Law (at high temperatures)

Notes on Questions

1. A power regression of our data shows a power of 4.36. However, an analysis of only those points with temperature greater than 1500° shows a power of 4.01. This inaccuracy in the low-temperature points is due to absorption of the infrared by the glass lamp bulb. (See experiment 1) This absorption is more significant at the lower temperatures, where the infrared makes up a larger percentage of the entire output.

---

Notes on Procedure

Part 1

3. Between readings, place the insulating material between the lamp and the sensor. For best results use both sheets, with the aluminum sides facing away from each other. Remove the sheets for only enough time to take each measurement.

Calculations

3/4

\[
f(x) = 5.521363 \times 10^{-14} \times x^{4.363707E+0} \\
R^2 = 9.979700E-1
\]
2 The lamp filament is not a true black body. If it were, it would be completely and totally black at room temperature. It is a fairly good approximation, though, as long as the temperature is high enough that the emitted light is much greater than the incident light.

3 Any other thermal source in the room would influence the results, including the warm body of the experimenter and the room itself. These introduce some error, but it is small as long as the temperature of the lamp is high compared to the temperature of these other sources.

### Experiment 4: Stefan-Boltzmann Law (at low temperatures)

#### Notes on Procedure

3 Make sure that the Thermal Radiation Cube has been off for enough time to be at equilibrium with the room before making this measurement. If the cube has been turned on recently, use another thermometer to make the measurement.

5 Use ridiculous precautions with this experiment. It is impossible to have too much insulation between the cube and the sensor between measurements. For our experiments, we use two foam sheets covered with aluminum tape, and an air gap between the sheets. We never removed this heat shield for more than 5 seconds while taking a measurement.

#### Calculations

![Graph showing the Stefan-Boltzmann equation](image)

\[ f(x) = 1.235365E-9x + -1.396775E-1 \]

\[ R^2 = 9.881626E-1 \]

#### Notes on Questions

1 The linearity of this graph indicates that the Stefan-Boltzmann equation is correct, even at low temperatures.

2 The graph should be straight, with some statistical variations.
Technical Support

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  Type of Computer (Make, Model, Speed).
  Type of external Cables/Peripherals.

• If your problem is with the PASCO apparatus, note:
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  Approximate age of apparatus.
  A detailed description of the problem/sequence of events. (In case you can't call PASCO right away, you won't lose valuable data.)
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  Part number and Revision (listed by month and year on the front cover).
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